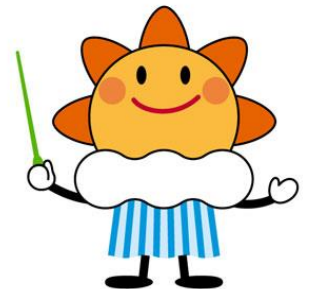


# Assessment of Future Climate Change Introduction to the Exercises

WAKAMATSU Shunya



# Table of Contents

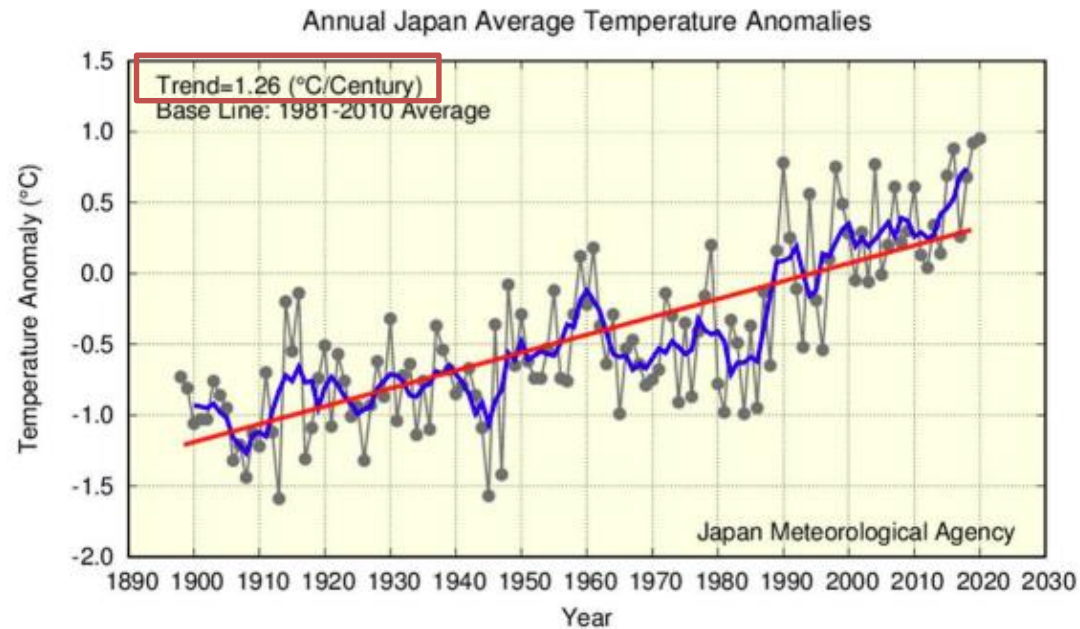
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1. How to calculate long-term trends in observation
2. How to calculate bias-corrected future changes
3. How to check the reliability

# Description of a long-term trend

## JMA Climate Change Monitoring Report 2020

- On a longer time scale, it is virtually certain that the annual mean surface temperature over Japan has risen at a rate of 1.26°C per century (statistically significant at a confidence level of 99%).

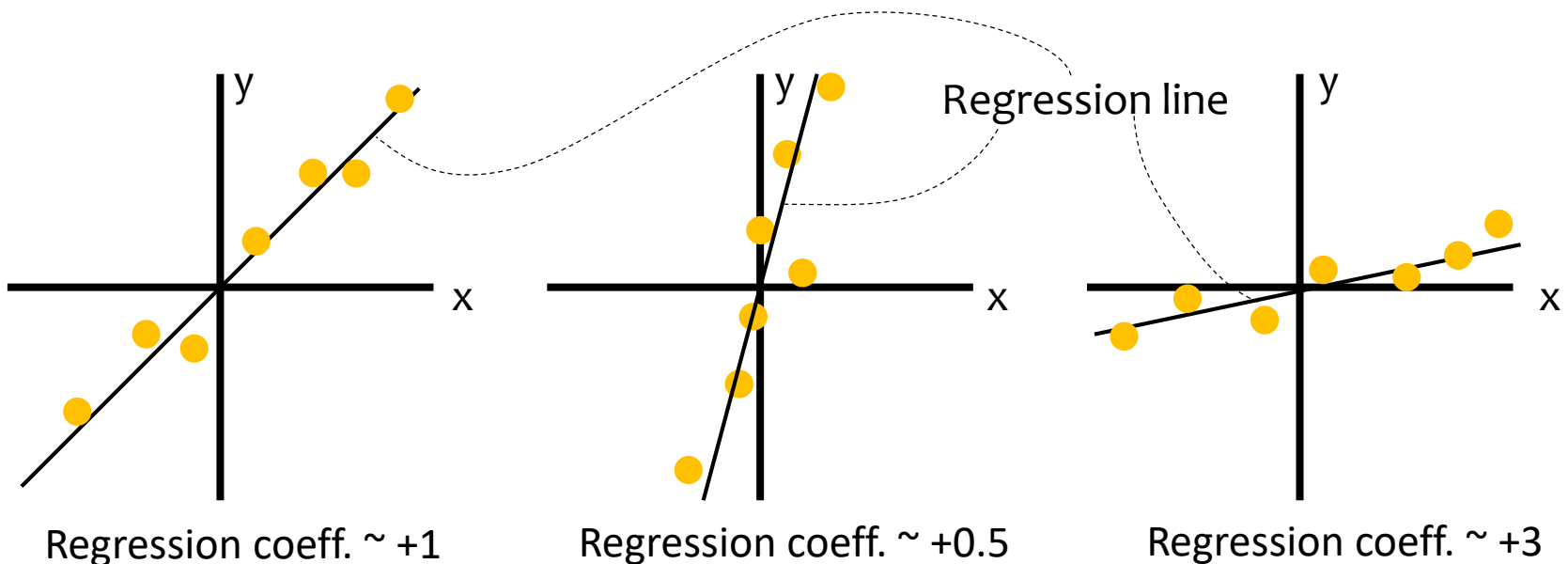


Long-term trend

Significant test

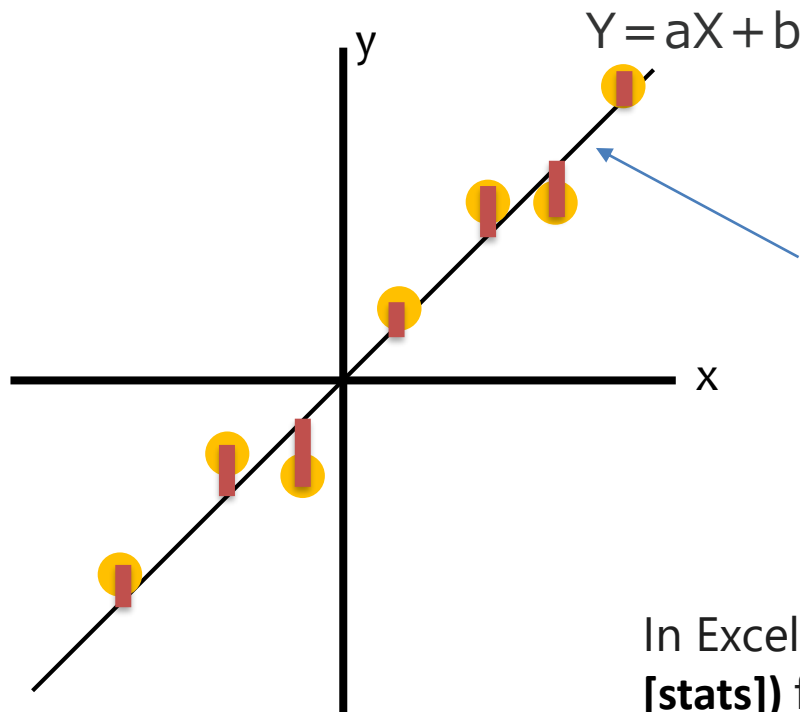
# Linear regression analysis

- When data has a linear relationship, a linear regression coefficient (a slope of a regression line) is data's trend.
- Since the slope is given by  $\Delta y/\Delta x$ , regression coefficients mean how much the variable  $y$  changes when the variable  $x$  changes.



## ■ Least-squares method

- a standard approach in linear regression analysis, by minimizing the sum of the squares of the residuals between observed values and the fitted values.



Residuals = 

Find the optimal linear model that minimizes the residuals (the error of estimation)

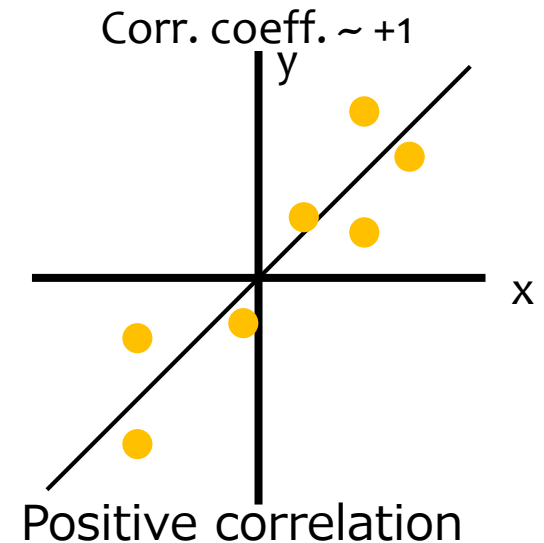
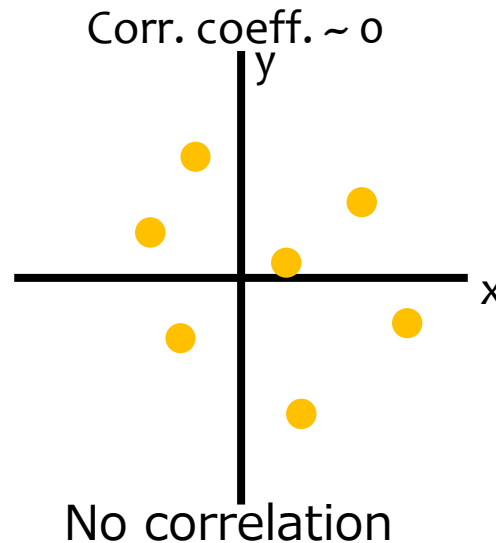
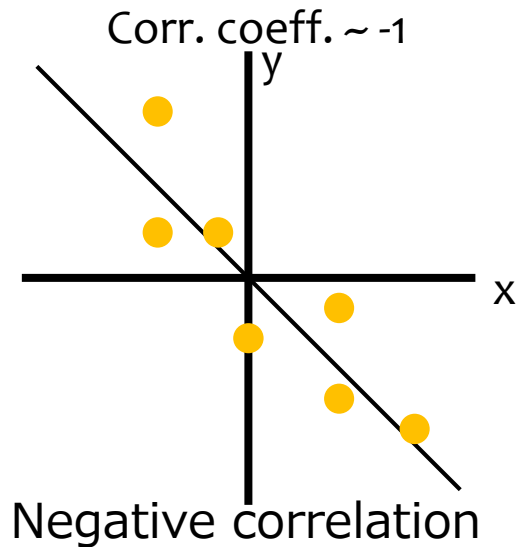
$$m = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

$$b = \bar{y} - m\bar{x}$$

In Excel, the **LINEST(known\_y's, [known\_x's], [const], [stats])** function returns the m-coefficients and the constant b.

# Correlation analysis

- Correlation coefficient: How close they have a linear relationship
  - Correlation coefficient values are between -1 and +1.
  - The value close to +1 (or -1) means there is a clear positive (negative) linear relationship between the targeted data pair, and the value around zero means there is little (or weak) relation between them.



## ■ Pearson correlation coefficient

- The ratio between the covariance of two variables and the product of their standard deviations (normalizing the covariance to a value between -1 and 1)

Covariance of x and y

$\frac{\text{Covariance of x and y}}{(\text{Standard deviation of x}) \times (\text{Standard deviation of y})}$

$x_i, y_i$ : single value of dependent variable

$\bar{x}, \bar{y}$ : mean of all values of independent variable

$n$ : population count

$$\begin{aligned} &= \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2}} \\ &= \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \end{aligned}$$

In Excel, the **CORREL(array1, array2)** function returns the correlation coefficient of two cell ranges.

# Statistical test (Student's $t$ -test)

- Does the long-term trend (=correlation) exist?
  - Null hypothesis: “the true correlation coefficient is equal to 0 (no correlation).”
  - Check whether the sample data are inconsistent with the null hypothesis or not
  - if they are inconsistent, then reject the null hypothesis (no correlation) and conclude that “the true correlation coefficient is not 0 (correlation exists)”.
  - If the underlying variables have a bivariate **normal distribution**, Since the sampling distribution of the specific correlation coefficient **T** (Pearson's correlation coefficient divided by the standard error) follows Student's **t-distribution** with degrees of **freedom n-2**, if t is significantly (e.g., 99%) unlikely to have occurred in the Student's t-distribution, the null hypothesis is rejected.

$$T = \frac{|r|\sqrt{n-2}}{\sqrt{1-r^2}}$$



# Type I and type II errors

- Even if the null hypothesis is rejected at a confidence level of 95%, this does not mean the decision is 100% correct.
- Type I error (false positive)
  - Rejecting the null hypothesis which is actually true in reality.
- Type II error (false negative)
  - Not rejecting the null hypothesis which is actually not true in reality.
- Neyman-Pearson lemma
  - Retaining a prespecified level of type I error, subsequently minimize type II error.
- Use the test with the most power at a prespecified confidence level
  - Usually, Student's *t*-test is the good choice.

		Decision about null hypothesis	
		reject	Don't reject
Null hypothesis is	Actually false	○	Type II error (false negative)
	Actually true	Type I error (false positive)	○

# Type III error

- Type III error (Another definitions also exist)
  - Choosing the test falsely to suit the significance of the sample.
- The assumptions underlying a  $t$ -test are:
  - Normality (Samples from Normal Distribution)
  - Independent samples (No autocorrelation. Past values does not affect future one)
  - Homogeneity of variance (from past to future)
- In general, precipitation data does not have normality.
  - If you choose  $t$ -test for precipitation, type III error occurs.
  - You have to choose one of the nonparametric statistics, which does not require the assumptions of normality.
    - E.g., Kendall rank correlation coefficient

# Kendall rank correlation coefficient

- Kendall rank correlation coefficient measure the ordinal association between two measured quantities.

(Example)

x	2001	2002	2003	2004	2005
y	1300	1350	1200	1250	1400

2001 -> 2003  
2001 -> 2004  
2002 -> 2003  
2002 -> 2004

(number of concordant pairs) =  $P = 6$       (number of discordant pairs) =  $Q = 4$

(number ways to choose ) =  ${}_n C_2 = \frac{n(n-1)}{2}$  The binomial coefficient

The Kendall  $\tau$  coefficient is defined as:  $\tau = \frac{P - Q}{\frac{n(n-1)}{2}} = \frac{6 - 4}{10} = 0.2$  When there are ties, the formula becomes more complicated! I recommend you use R software.

With the independence and larger samples of X and Y, it is common to use an approximation to the normal distribution, with mean zero and variance  $\frac{2(2n+5)}{9n(n-1)}$

Therefore, we can conduct statistical test with a standard normal distribution with the modified  $\tau$ .

To be precise, this value is incorrect because of its small sample size. You can calculate the exact value by using R software.

$$\frac{\tau}{\sqrt{\frac{2(2n+5)}{9n(n-1)}}} \sim 0.49$$

# Description of future change

- In general, future changes of climate are described as the difference of climate model outputs between present and future.
  - In this training seminar, we use MRI-AGCM3.2 as the model.

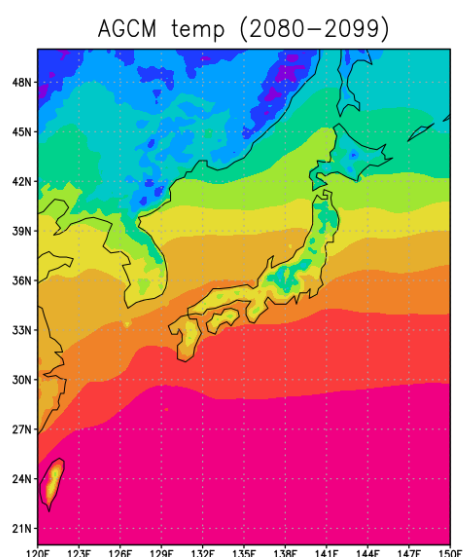
Future (Climate model)



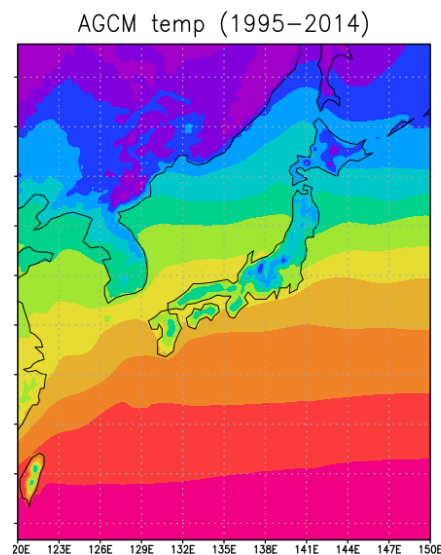
Present (Climate model)



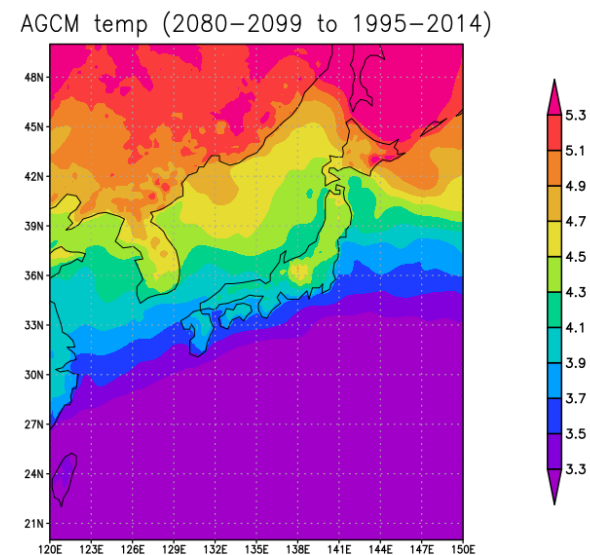
Future change (F-P)



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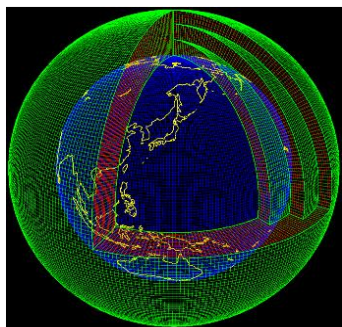


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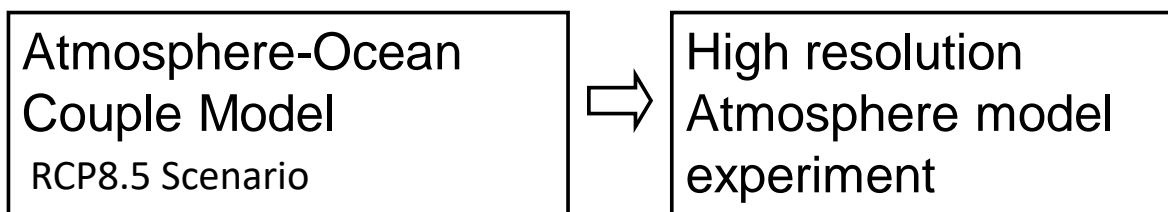
Projection by MRI-AGCM3.2S based on RCP8.5

# About MRI-AGCM projection data

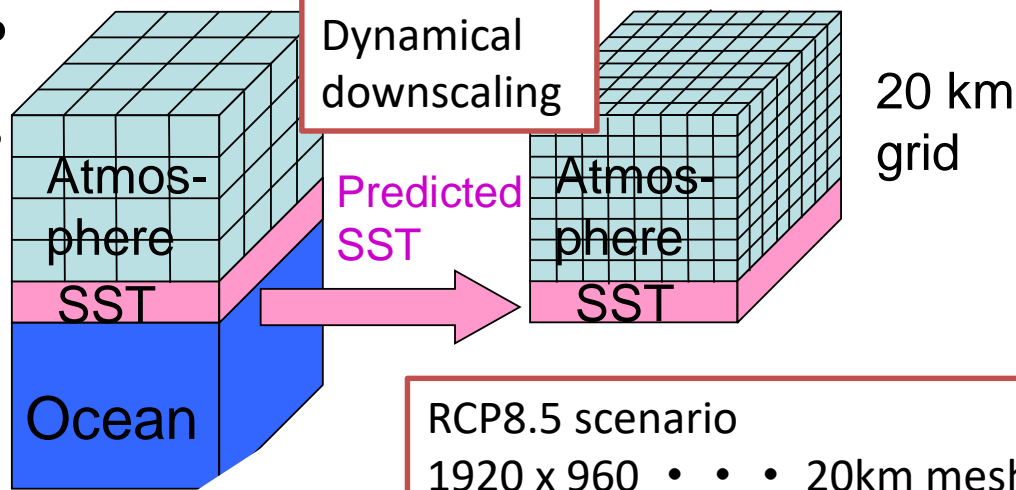
- MRI-AGCM3.2S, the model joining in the CMIP6 (HighResMIP).



MRI-AGCM projection Data

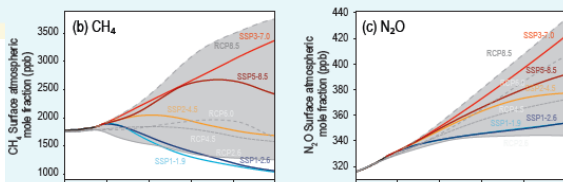
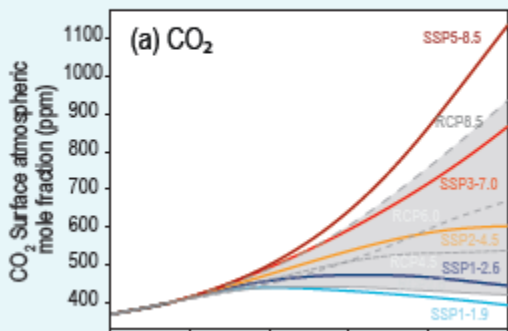


WCRP  
CMIP5



RCP8.5 scenario  
1920 x 960 • • • 20km mesh !!





SSP and RCP concentrations




AR6 WG1 Cross-Chapter Box 1.4, Figure 2

# How to obtain MRI-AGCM projection data

Data can be obtained from the WCRP website.

Hosted by   Powered by  and 

Welcome, Guest | Login | Create Account



You are at the [ESGF-DATA.DKRZ.DE](#) node [Technical Support](#)

MIP Era

- CMIP6 (4)

Activity

- HighResMIP (4)

Model Cohort

Product

WARNING: Not all models include a variant 'r1i1p1f1' and across models, identical values of variant\_label do not imply identical variants! To learn which forcing datasets were used in each variant, please check modeling group publications and documentation provided through ES-DOC.

Enter Text:    Display  results per page [More Search Options](#)

Search Constraints:  CMIP6 |  HighResMIP |  MRI |  MRI-AGCM3-2-S |  pr:tas |  mon

Total Number of Results: 4

*Please login to add search results to your Data Cart*  
Expert Users: you may display the search URL and return results as XML or return results as JSON

- CMIP6.HighResMIP.MRL.MRI-AGCM3-2-S.highresSST-present.r1i1p1f1.Amon.tas.gn  
Data Node: esgf-data2.diasjp.net  
Version: 20190711  
Total Number of Files (for all variables): 4  
Full Dataset Services: [Show Metadata](#) | [List Files](#) | [THREDDS Catalog](#) | [WGET Script](#) | [Show Citation](#) | [PID](#) | [Further Info](#)
- CMIP6.HighResMIP.MRL.MRI-AGCM3-2-S.highresSST-present.r1i1p1f1.Amon.pr.gn

<https://esgf-data.dkrz.de/search/cmip6-dkrz/>

Source ID

- MRI-AGCM3-2-S (4)

Institution ID

- MRI (4)

Source Type

Nominal Resolution

Experiment ID

Sub-Experiment

Variant Label

Grid Label

Table ID

Frequency

- mon (4)

Realm

Variable

- pr (2)
- tas (2)

CF Standard Name

File Name	Content
tas_Amon_MRI-AGCM3-2-S_highresSST-future_r1i1p1f1_gn_207101-209012.nc tas_Amon_MRI-AGCM3-2-S_highresSST-future_r1i1p1f1_gn_209101-209912.nc	AGCM temperature (monthly, future) [K]
tas_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_199001-200912.nc tas_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_201001-201412.nc	AGCM temperature (monthly, present) [K]
File Name	Content
pr_Amon_MRI-AGCM3-2-S_highresSST-future_r1i1p1f1_gn_207101-209012.nc pr_Amon_MRI-AGCM3-2-S_highresSST-future_r1i1p1f1_gn_209101-209912.nc	AGCM precipitation (monthly, future) [kg m-2 s-1]
pr_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_199001-200912.nc pr_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_201001-201412.nc	AGCM precipitation (monthly, present) [kg m-2 s-1]

# How to obtain MRI-AGCM projection data

- By using GrADS or OpenGrADS, time series of output values can be obtained easily.

- However, the operation of GrADS or OpenGrADS is beyond the scope of this training seminar.
- In this training seminar, simplified csv data prepared by lecturer will be provided for time saving.



Grid Analysis and Display  
System  
(GrADS)



OpenGrADS

"Opening GrADS to a World of Extensions"

<http://cola.gmu.edu/grads/>  
<http://opengrads.org/>

```
ga-> sdfopen temp/tas_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_199001-200912.nc
ga-> set lon 139.75
ga-> set lat 35.69
ga-> set gxout print
ga-> set prnopts %7.3f 1 1
ga-> set time jan1995 dec2009
ga-> d tas
```

Longitude and Latitude Setting

Open a file

Print format

Set time range and Draw

```
ga-> sdfopen temp/pr_Amon_MRI-AGCM3-2-S_highresSST-present_r1i1p1f1_gn_199001-200912.nc
ga-> set lon 139.75
ga-> set lat 35.69
ga-> set gxout print
ga-> set prnopts %10.3e 1 1
ga-> set time jan1995 dec2009
ga-> d pr
```

# Concerns when describing the future change

- In general, future changes of climate are described as the difference of climate model outputs between present and future.
  - There are several points to be included into consideration.

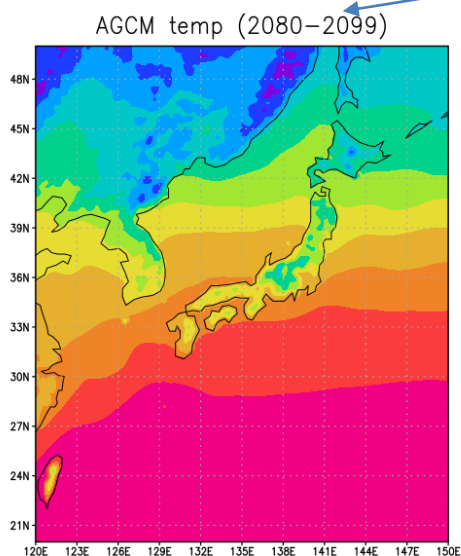
Future (Climate model)

Present (Climate model)

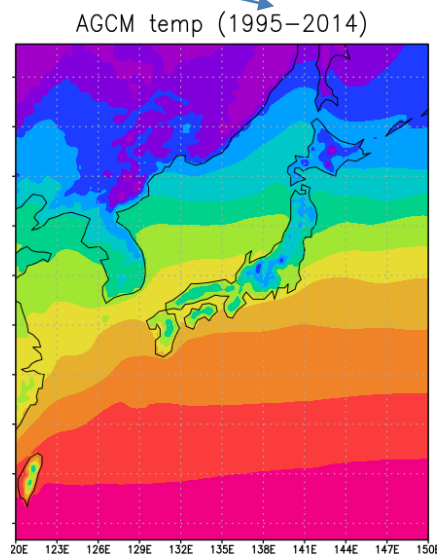
Future change (F-P)

Mean climate state?

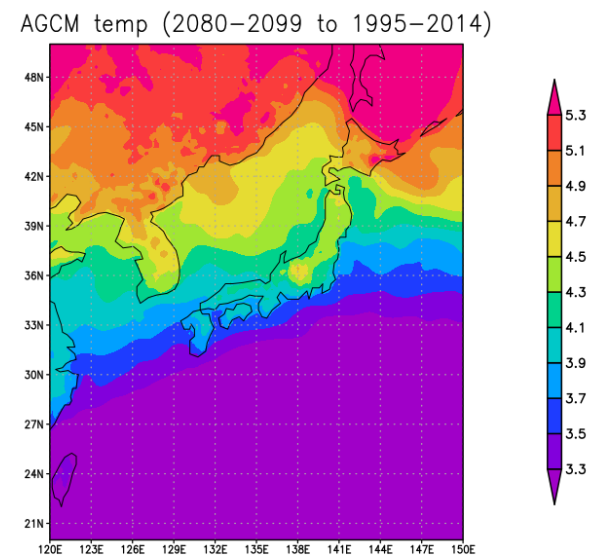
Realistic?



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2022-06-06-10:11



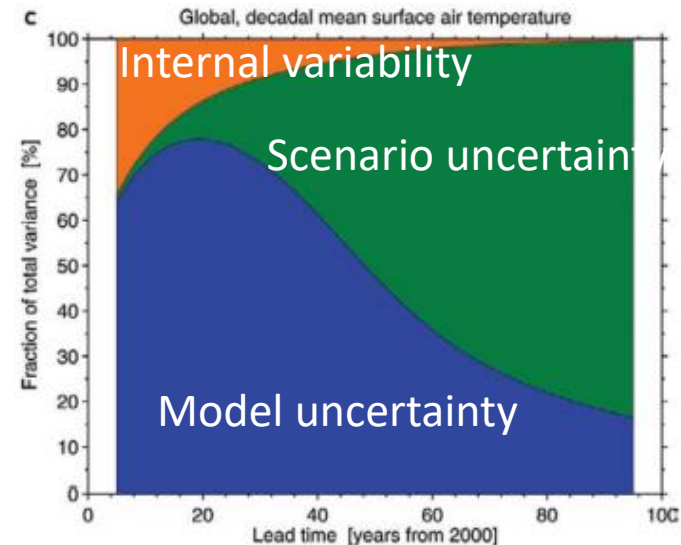
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Projection by MRI-AGCM3.2S based on RCP8.5

Reliable?

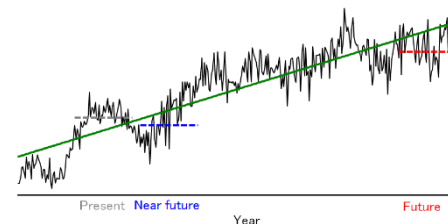


- Global warming projection contains many uncertainties. Therefore, we cannot say the results are correct projections without considering the uncertainties.
- Types of uncertainty
  - Natural climate variability
  - Regional scale
  - Incompleteness of climate model
  - Short period for calculation

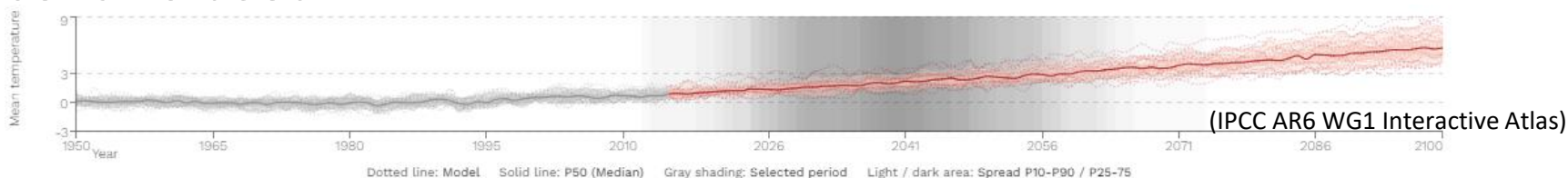


(Hawkins and Sutton 2009)

- The aim is to project climate change signals rather than natural climate variability.
  - Even state-of-the-art climate models cannot predict natural variability.
  - The 20-year average of results from the climate model are used for global warming projection.
- Uncertainties in regional-scale climate projections are greater than those in global-scale climate projections.
  - It is necessary to examine whether projected regional-scale climate change is consistent with broader-scale climate change.
- Uncertainties in near-future climate projections are larger than those in future climate projections.
  - As the level of greenhouse gas concentration in near-future projections is expected to be lower than that in future projections, less pronounced climate change signals may be dominated by natural variability.



- Uncertainties exist even in long-term trends.
  - Future climate projection uncertainties can be estimated via multi-model or multi-parameter experiments.
- The ability of models to project future climate conditions is limited.
  - Large-scale patterns averaged over a broader area provide a more meaningful picture than changes on a single-grid scale.
- Uncertainties in future projections depend on the variables used.
  - Detecting climatological trends for precipitation is more difficult than that for temperature because extreme rainfall events are rare by definition and occur on relatively limited spatial and temporal scales.
- Future projections depend on the greenhouse gas emissions scenario used.



# Tackle the uncertainty (example)

## ■ Natural climate variability

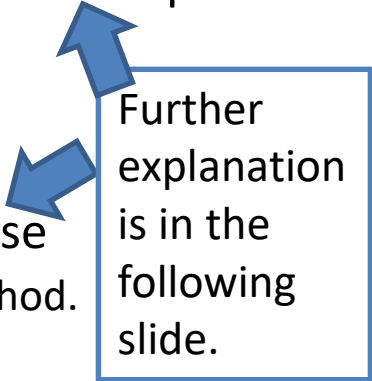
- Choose longer mean period than natural variability
  - In this training seminar, we choose 20-years mean

## ■ Regional scale

- Check the regional response as a part of the wider area
  - In this training seminar, we check the wider response by IPCC reports.

## ■ Incompleteness of climate model (Model bias)

- Check the reproducibility of the model
  - Take some bias correction method to correct the response
    - In this training seminar, we take a simple bias correction method.



Further explanation is in the following slide.

## ■ Short period for calculation

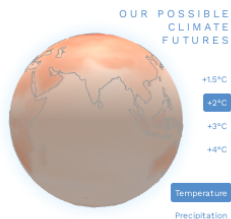
- See the long-term climate change in the model
  - In this training seminar, we see the response at the end of 21<sup>st</sup> century.


# Comparing the regional response with the wider response: How to get the value from IPCC WG1 Interactive Atlas

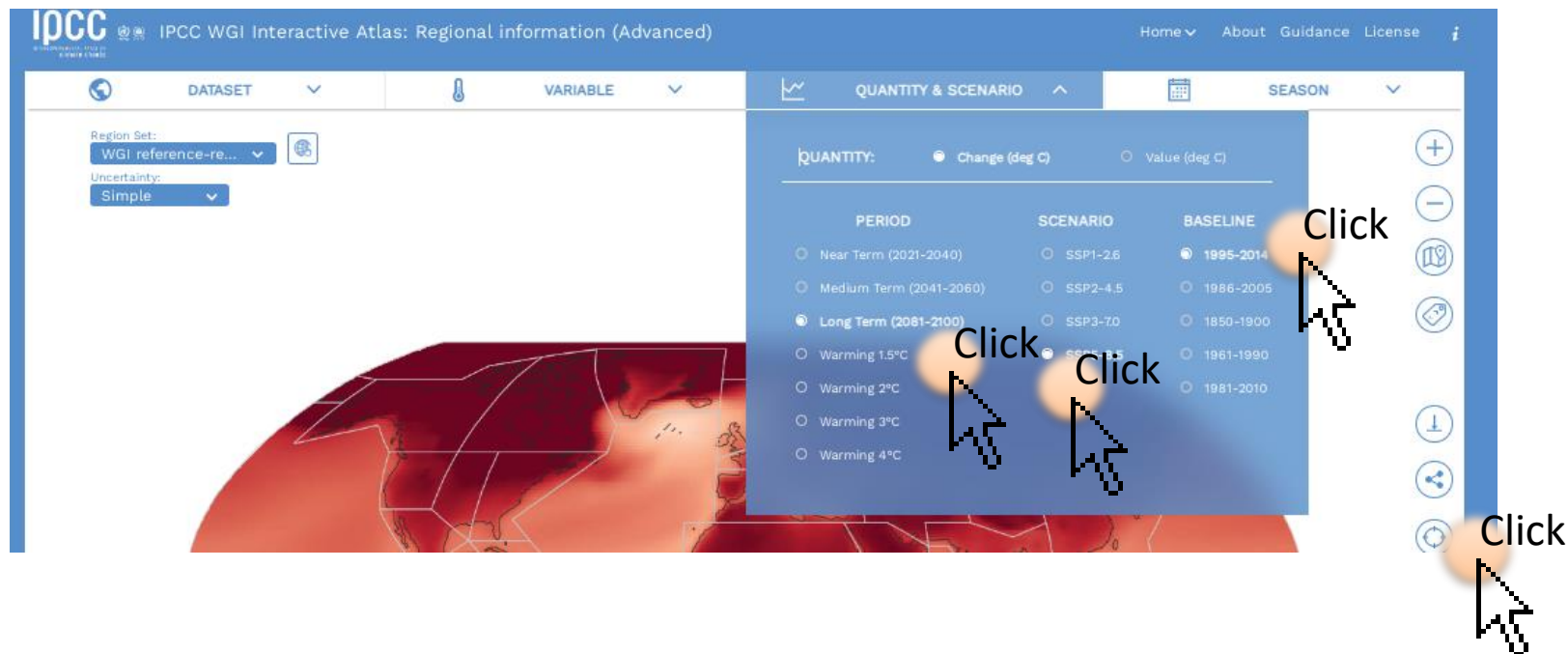
## IPCC WGI Interactive Atlas

A novel tool for flexible spatial and temporal analyses of much of the observed and projected climate change information underpinning the Working Group I contribution to the Sixth Assessment Report, including regional synthesis for Climatic Impact-Drivers (CIDs).

Participate in the user testing survey [↗](#) | [Errata and problem reporting](#) | [License and citation](#) | [Contact](#)



- Go to the website
  - <https://interactive-atlas.ipcc.ch/>
- Click “Advanced”
- Hover over “Quantity & Scenario”
- Click “Long Term (2081-2100)”
- Click “SSP8-8.5”
- Click “1995-2014”
- Click “Point Information” 
- Click the point in your country/region



ipcc IPCC WGI Interactive Atlas: Regional information (Advanced)

Home About Guidance License

DATASET VARIABLE QUANTITY & SCENARIO SEASON

Region Set: WGI reference-re...  
Uncertainty: Simple

QUANTITY: Change (deg C) Value (deg C)

PERIOD	SCENARIO	BASELINE
<input type="radio"/> Near Term (2021-2040)	<input type="radio"/> SSP1-2.6	<input checked="" type="radio"/> 1995-2014
<input type="radio"/> Medium Term (2041-2060)	<input type="radio"/> SSP2-4.5	<input type="radio"/> 1986-2005
<input checked="" type="radio"/> Long Term (2081-2100)	<input type="radio"/> SSP3-7.0	<input type="radio"/> 1850-1900
<input type="radio"/> Warming 1.5°C	<input checked="" type="radio"/> SSP8-8.5	<input type="radio"/> 1961-1990
<input type="radio"/> Warming 2°C		<input type="radio"/> 1981-2010
<input type="radio"/> Warming 3°C		
<input type="radio"/> Warming 4°C		

Click

Click

Click

Click

- Bias (systematic errors) in climate models is defined as certain tendency for errors in climate models.
  - E.g., the model tends to project warmer than observation (positive bias).
- The reproducibility can be judged by calculating the bias. Bias can be defined here as **Simulation** minus **Observation**.
  - **Simulation** is the forecast which is conducted by climate models.
  - **Observation** is the values which the model tries to reproduce.
- Simulation and Observation cannot be exactly the same result. **Every model has its own bias.**
  - Arising from simplified physics, parameterizations, rack of resolution and so on.
- Bias correction is the way to overcome the problem, which adjusts present simulation to observation. For example, a simple way (Delta method) is:
  - (Temp.)  $\text{Future}_{\text{Bias corrected}} = \text{Observation} + \text{Future} - \text{Present}$
  - (Precip.)  $\text{Future}_{\text{Bias corrected}} = \text{Observation} * \left(\frac{\text{Future}}{\text{Present}}\right)$